

1 **Seasonal and interannual variation in spatio-temporal models**
2 **for index standardization and phenology studies**

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20 **Abstract:**

21 Climate change is rapidly affecting the seasonal timing of spatial demographic processes.
22 Consequently, resource managers require information from models that simultaneously measure
23 seasonal, interannual, and spatial variation. We present a spatio-temporal model that includes
24 annual, seasonal, and spatial variation in density and then highlight two important uses: (1)
25 standardizing data that are spatially unbalanced within multiple seasons; and (2) identifying
26 inter-annual changes in seasonal timing (“phenology”) of population processes. We demonstrate
27 these uses with two contrasting case studies: three bottom trawl surveys for yellowtail flounder
28 (*Limanda ferruginea*) in the Northwest Atlantic Ocean from 1985-2017, and pelagic tows for
29 copepodite stage 3+ copepod (*Calanus glacialis/marshallae*) densities in the eastern Bering Sea
30 from 1993-2016. The yellowtail analysis illustrates how data from multiple surveys can be used
31 to infer density hot spots in an area that is not sampled one or more surveys. The copepod
32 analysis assimilates seasonally unbalanced samples to estimate an annual index of the seasonal
33 timing of copepod abundance, and identifies a positive correlation between this index and cold-
34 pool extent. We conclude by discussing additional potential uses of seasonal spatio-temporal
35 models and emphasize their ability to identify climate-driven shifts in the seasonal timing of fish
36 movement and ecosystem productivity.

37

38 **Introduction**

39 Resource surveys are conducted worldwide to track changes in abundance for managed
40 species. These surveys are typically designed by management agencies to support a participatory
41 management process, where regulations are developed, proposed, and evaluated over the course
42 of several months or years. As a consequence, resource surveys are often designed to index
43 variation on the same interannual time-scale as management operates, typically occurring over a
44 fixed time-interval in each year. Well-known examples include the Christmas count survey for
45 birds in North America (Butcher *et al.*, 1990), or the spring and fall fishery resource surveys
46 conducted annually in the Northwest Atlantic Ocean from 1963 to present day (Grosslein, 1969;
47 Politis *et al.*, 2014). By occurring at the same time each year, this design is a powerful way to
48 control for within-year shifts in species distribution while maximizing statistical power for
49 detecting interannual variation in abundance.

50 Despite this common emphasis on capturing interannual variation in resource abundance,
51 there are many reasons to study changes occurring within a single year. For example, many
52 terrestrial and aquatic animals undergo a seasonal migration that partitions habitats available for
53 feeding and raising young, or follow ontogenetic movement patterns associated with distinct life
54 stages (e.g., immature vs. mature). The spatial extent and timing of these seasonal migrations
55 may shift over time, either due to changes in land use (Zipkin *et al.*, 2012) or environmental
56 conditions (Nichol *et al.*, 2019). Detecting these shifts in seasonal migration typically require
57 data (either via individual tracks or population counts) that arise across multiple seasonal
58 periods. In particular, the timing of different population processes (“phenology”) is predicted to
59 be a sensitive indicator of climate impacts (Scranton and Amarasekare, 2017), so detecting
60 climate-driven shifts in seasonal processes is a high priority for climate-impact studies.

61 Furthermore, there is a growing interest in leveraging citizen-science and other opportunistic
62 data sources (Callaghan *et al.*, 2018), and proper interpretation of these data sets requires
63 accounting for variation in population density among seasons.

64 In addition to studies detecting climate impacts on phenology, there is also a growing
65 literature documenting shifts in spatial distribution that are associated with local and regional
66 climate conditions (Pinsky *et al.*, 2013). Shifts in spatial distribution can be estimated using
67 spatio-temporal models (e.g., Thorson, 2019a), which estimate a “latent” (unobserved) map of
68 population densities across space and how this map of density changes over time (Cressie and
69 Wikle, 2011). Importantly, these spatio-temporal models typically include a spatial correlation
70 function, which allows densities to be predicted even at locations where sampling does not occur
71 (Cressie *et al.*, 2009). Density predictions arising from spatially unbalanced sampling may be
72 biased when sampling locations are not “missing at random”; that is, the probability of sampling
73 is correlated with the density occurring at a given location (Cressie *et al.*, 2009; Conn *et al.*,
74 2017). Nevertheless, spatio-temporal models for spatially unbalanced data can still mitigate bias
75 arising from ignoring the spatial configuration of data, where changes in the spatial distribution
76 of sampling would otherwise be confounded with changes in population density (Thorson *et al.*,
77 2016a).

78 While scientific surveys follow a defined sampling design and aim to maintain consistent
79 protocols, there are uncontrollable circumstances that can disrupt this design. For example,
80 severe weather, mechanical problems with the ship, and constraints arising from multiple
81 objectives and/or budget cuts can lead to greatly reduced or incomplete sampling of survey strata
82 in a given year. As a result, it becomes difficult to interpret interannual trends in abundance for
83 years when the design is not followed. In stock assessments for marine species, an analyst might

84 choose to exclude, downweight, or perform an *ad hoc* expansion for those incompletely sampled
85 years. By contrast, a seasonal spatio-temporal model could use sampling information from
86 another survey to inform about abundance in unsampled or poorly sampled areas. Similarly,
87 surveys of within-season changes in abundance or phenology will sometimes depart from their
88 design, or the design will shift over time. In these cases, it becomes necessary to simultaneously
89 correct for spatial and seasonal patterns in abundance when interpreting seasonally and spatially
90 unbalanced sampling data. While past studies have developed models that account for seasonal
91 variation when forecasting annual changes in abundance (e.g., Grieve *et al.*, 2017; Kanamori *et*
92 *al.*, 2019), these studies have not typically demonstrated the potential to assimilate seasonally
93 unbalanced sampling data (although see Pinto *et al.* (2018) for one exception).

94 In this study, we illustrate how to assimilate spatially and seasonally unbalanced sampling
95 data using a spatio-temporal model that includes both changes in spatial distribution among years
96 (interannual variation) and among seasons (seasonal variation). Models including both spatial
97 and temporal variation are often termed “spatio-temporal models.” We start by describing a
98 default configuration of our proposed seasonal spatio-temporal model, which includes seasonal
99 and annual main effects and an autocorrelated season-year effect for both intercepts and spatial
100 variation within a delta-modelling framework. This configuration preserves correlations in
101 spatial distribution among seasons for a given year (e.g., annual drivers of distribution), among
102 years for a given season (e.g., seasonal migratory patterns), and among adjacent seasons within
103 and across years (e.g., transient hotspots in spatial distribution). Previous spatio-temporal
104 models have typically included either interannual variation (e.g., Ono *et al.*, 2018) or seasonal
105 variation (e.g., Thorson *et al.*, 2016b; Grieve *et al.*, 2017) in isolation. Alternatively, a few
106 studies have modeled residual variation in spatial distribution among seasons and years.

107 However, these have not modeled the full set of correlations we consider in this study, e.g.,
108 without correlations among years for a given season (Pinto *et al.*, 2018), without correlations
109 among seasons for a given year (Kai *et al.*, 2017), or without information about the sequence of
110 seasons within a given year (Kanamori *et al.*, 2019). We then demonstrate model performance
111 using two contrasting case-studies: (1) standardizing seasonal indices of abundance for a
112 commercially important fish in the Northwest Atlantic, and (2) estimating interannual changes in
113 phenology for a planktonic crustacean in the northeast Pacific. These two case-studies highlight
114 our ability to share information among seasons to account for spatially unbalanced sampling
115 among years and seasons, and to identify changes in seasonal dynamics over time.

116 **Methods**

117 **Model structure**

118 We seek to develop a statistical model that represents spatial variation in population density, and
119 how density changes both among years (“interannual variation”) and within years (“seasonal
120 variation”). We envision that field-sampling data are available, where sample b_i records the
121 biomass (kg) or abundance (numbers) encountered by the i -th sample, occurring at location s_i
122 (within a fixed and pre-defined spatial domain), year y_i (between a minimum and maximum year
123 $y \in \{y_{min}, \dots, y_{max}\}$), and season u_i (among an ordered set of intervals occurring within a year,
124 $u_i \in \{u_1, \dots, u_U\}$). These seasons could be quarters (winter, spring, summer, fall), months
125 (January-December), weeks (1-52), or any intervals defined within a year (whether having even
126 or uneven spacing and duration). In this notation, the combination of year y_i and season u_i is
127 sufficient to define the time of a given sample, and the term t to describe this combination, $t \in$
128 $\{y_{min}u_1, y_{min}u_2, \dots, y_{max}u_U\}$, where seasons and years are ordered such that $t + 1$ is the year-

129 season combination occurring immediately after t and $t - 1$ is the year-season combination
 130 preceding t . We note that densities can change rapidly within a given year and encourage future
 131 studies to explore different intervals for season u , as we do in the following case study for
 132 copepod densities.

133 In particular, we seek a model that has reasonable performance even when data are entirely
 134 unavailable for one or more combinations of year and season. In these instances, we specify that
 135 estimates in year-season t are shrunk towards predicted density in adjacent year-seasons ($t - 1$
 136 and $t + 1$), as well as towards estimated density in other seasons for a given year (other u for a
 137 given y) and density in other years for a given season (other y for a given u). This specification
 138 implies that the model will include a “main effect” for season and year, as well as an
 139 autocorrelated “interaction” of season and year.

140 We implement these criteria using a Poisson-link delta model (Thorson, 2018) that specifies
 141 a probability distribution for random variable B , corresponding to the likelihood of response
 142 variable b_i for each sample i , $\Pr(B = b_i)$. This Poisson-link delta model includes the
 143 probability p_i that sample i encounters a given species (i.e., $\Pr(B > 0)$), and also the expected
 144 measurement r_i given that the species is encountered, $\Pr(B|B > 0)$:

$$\Pr(B = b_i) = \begin{cases} 1 - p_i & \text{if } B = 0 \\ p_i \times g\{B|r_i, \sigma_m^2\} & \text{if } B > 0 \end{cases} \quad (1)$$

145 where we specify a lognormal distribution for the distribution g of positive catches. This
 146 Poisson-link delta model predicts encounter probability p_i and positive catch rate r_i by modelling
 147 two log-linked linear predictors, $\log(n_i)$ and $\log(w_i)$ for each sample i ; n_i and w_i are then
 148 transformed to yield p_i and r_i :

$$p_i = 1 - \exp(-a_i \times n_i) \quad (2)$$

$$r_i = \frac{a_i \times n_i}{p_i} \times w_i$$

149 where a_i is the area-swept offset for sample i . This model structure is designed such that
 150 expected density d_i is the product of encounter probability and positive catch rate, and also the
 151 product of transformed linear predictors (i.e., $d_i = p_i r_i = n_i w_i$). When the response-variable b_i
 152 is in units biomass, these predictors can be interpreted as numbers density n_i (with units numbers
 153 per area) and average weights w_i (with units biomass per number). Alternatively, if the response-
 154 variable is in units numbers, n_i (with units numbers per area) and w_i (with dimensionless units)
 155 describe a parametric link between expected encounter probability and expected numbers given
 156 an encounter, but they are not specifically interpretable as describing numbers-density and
 157 biomass per number. In both interpretations, n_i always enters via the product $a_i \times n_i$ such that
 158 n_i is expressed as density.

159 The Poisson-link delta model is useful relative to other delta-models because both linear
 160 predictors use a log-link function, so that all effects are additive in their impact on predicted log-
 161 density. Specifically, we specify that:

$$\log(n_i) = \underbrace{\beta_n^*(t_i)}_{\text{Year-Season intercept}} + \underbrace{\omega_n^*(s_i)}_{\text{Spatial main effect}} + \underbrace{\xi_{nu}^*(s_i, u_i)}_{\text{Season spatial effect}} + \underbrace{\xi_{ny}^*(s_i, y_i)}_{\text{Year spatial effect}} + \underbrace{\varepsilon_n^*(s_i, t_i)}_{\text{Year-Season spatial effect}} \quad (3)$$

162 where the other linear predictor w_i is defined identically except that the subscript n is replaced
 163 by w for all coefficients. In applications with limited information (either due to low sample sizes
 164 or small variance), the variance of one or more of these terms may be estimated near zero such
 165 that the corresponding term is then dropped from the model. Specifying an additive structure in

166 log-space for both variables (n_i and w_i) simplifies interpretation of estimated terms where, e.g.,
 167 $\omega_n^*(s_1) = 0.1$ indicates that $n(s_1, t)$ is expected to be 10% higher at location s_1 than at location
 168 s_2 where $\omega_n^*(s_2) = 0$. We also hypothesize that this additive structure in log-space will be more
 169 parsimonious than a conventional delta-model, although testing this is an empirical question for
 170 future research.

171 Spatial terms are estimated using a predictive-process framework (Banerjee *et al.*, 2008),
 172 such that we estimate the value of each spatial variable at a set of “knots,” where the number of
 173 knots n_x is specified by the user in a balance between computational speed and spatial
 174 resolution. In the case of spatial variation, we specify a Gaussian Markov random field for
 175 vector ω_n^* containing the value of the spatial variable $\omega_n(s)$ at each knot s :

$$\omega_n \sim MVN(\mathbf{0}, \sigma_{n\omega}^2 \mathbf{R}_n) \quad (4)$$

176 where \mathbf{R}_n is the correlation matrix and $\sigma_{n\omega}^2$ is the pointwise variance such that $\sigma_{n\omega}^2 \mathbf{R}_n$ is the
 177 spatial covariance. We then project from the values ω_n at knots to the values ω_n^* at the location
 178 of available data. The correlation matrix, in turn, is calculated based on a vector of distance
 179 $\mathbf{d}(s_1, s_2)$ between any pair of locations s_1 and s_2 , and we use a sparse precision matrix that
 180 approximates a Matérn correlation function (Lindgren *et al.*, 2011):

$$\mathbf{R}_n(s_1, s_1) = \frac{1}{2^{\nu-1} \Gamma(\nu)} \times (\kappa_n |\mathbf{d}(s_1, s_2) \mathbf{H}|)^\nu \times K_\nu(\kappa_n |\mathbf{d}(s_1, s_2) \mathbf{H}|) \quad (5)$$

181 where we estimate a linear transformation \mathbf{H} involving estimated parameters (representing
 182 geometric anisotropy) and decorrelation rate κ_n . Given the value of a spatial variable at each
 183 knot, the value at any given location s within spatial domain Ω is then calculated using bilinear
 184 interpolation, using a projection matrix calculated by the R package R-INLA (Lindgren, 2012).

185 Season and year main spatial effects are specified similarly, except the probability of $\xi_{nu}(u)$ is
 186 calculated independently for every season u , and the probability of $\xi_{ny}(y)$ is calculated
 187 independently for every year y . However, the year-season interaction $\epsilon_n(s, t)$ is autocorrelated
 188 across the ordered year-season index t :

$$\epsilon_n(s, t) \sim \begin{cases} MVN(\mathbf{0}, \mathbf{Q}^{-1}) & \text{if } t = t_{min} \\ MVN(\rho_{n\epsilon}\epsilon_n(s, t-1), \mathbf{Q}^{-1}) & \text{if } t > t_{min} \end{cases} \quad (6)$$

189 where the degree of autocorrelation $\rho_{n\epsilon}$ in spatio-temporal variation $\epsilon_n(s, t)$ is also estimated.
 190 We here assume that the decorrelation-rate parameters κ_n and κ_w are identical for spatial and
 191 spatio-temporal components and different between the two linear predictors n and w ; future
 192 research could explore alternative specification for these hyperparameters.

193 Similarly, intercepts $\beta_n(t)$ are specified such that they can be interpolated for season-year
 194 combinations without any data using information from adjacent season-years, other years of the
 195 same season, or other seasons of the same year. This is again accomplished by including season
 196 and year main effects, and an autocorrelated interaction of season and year:

$$\beta_n^*(t) = \mu_\beta + \beta_{nu}(u) + \beta_{ny}(y) + \beta_{nt}(t) \quad (7)$$

197 Where μ_β is the average intercept across all seasons and years, $\beta_{nu}(u)$ captures differences in
 198 expected intercept among seasons u , $\beta_{ny}(y)$ captures differences in expected intercepts among
 199 years y , and $\beta_{nt}(t)$ represents an autocorrelated season-year interaction:

$$\beta_{nt}(t) \sim \begin{cases} N(0, \sigma_{n\beta}^2) & \text{if } t = t_{min} \\ N(\rho_{n\beta}\beta_{nt}(t-1), \sigma_{n\beta}^2) & \text{if } t > t_{min} \end{cases} \quad (8)$$

200 and where the magnitude of autocorrelation is again estimated from available data. We ensure
 201 identifiability for μ_β , $\beta_{nu}(u)$, and $\beta_{ny}(y)$ by imposing a corner constraint on the season and year

202 effects (i.e., $\beta_{nu}(u) = 0$ and $\beta_{ny}(y) = 0$ for the first season u and year y). This corner
 203 constraint is necessary for intercepts (i.e., Eq. 7) but not spatial terms (i.e., Eq. 3) because the
 204 season and year intercepts are treated as fixed effects, while the season and year spatial terms are
 205 treated as random effects. We note that this model structure imposes no constraints on the
 206 expected “shape” of seasonal variation; that is, the model can capture unimodal or multi-modal
 207 distribution of abundance across seasons within a year.

208 Parameters are estimated using release 3.2.0 of package VAST (Thorson, 2019b), which is
 209 publicly available online (<https://github.com/James-Thorson/VAST>), and runs within the R
 210 statistical environment (R Core Team, 2017). The performance of VAST for models such as this
 211 has been simulation-tested previously (Thorson *et al.*, 2015, 2016a; Grüss *et al.*, 2019; Johnson
 212 *et al.*, 2019; Brodie *et al.*, 2020), and we recommend future simulation experiments exploring
 213 performance for the specific seasonal structure proposed here. VAST estimates fixed effects
 214 while approximating their marginal likelihood using the Laplace approximation (Skaug and
 215 Fournier, 2006). The Laplace approximation is implemented in turn using R package TMB
 216 (Kristensen *et al.*, 2016), and computational efficiency is improved using automatic
 217 differentiation (Fournier *et al.*, 2012) and the SPDE approximation to spatial correlation matrices
 218 (and associated projection matrices) from R-INLA (Lindgren and Rue, 2015). Standard errors
 219 are calculated using a generalization of the delta-method (Kass and Steffey, 1989), and standard
 220 errors are available for predictions of local density after estimating all fixed and random effects:

$$\begin{aligned}
 d(s, t) &= n(s, t) \times w(s, t) && (9) \\
 &= \exp\{\beta_n^*(t) + \omega_n^*(s) + \xi_{nu}^*(s, u) + \xi_{ny}^*(s, y) + \varepsilon_n^*(s, t)\} \\
 &\times \exp\{\beta_w^*(t) + \omega_w^*(s) + \xi_{wu}^*(s, u) + \xi_{wy}^*(s, y) + \varepsilon_w^*(s, t)\}
 \end{aligned}$$

221 where density can then be visualized or further processed to yield derived statistics. For
222 example, total abundance is calculated as the area-weighted sum of density $d(s, t)$ predicted at a
223 fine spatial resolution:

$$D(t) = \sum_{s=1}^{n_s} a(s)d(s, t) \quad (10)$$

224 Where n_s is the number of fine-scale predictions and $a(s)$ is the spatial area associated with each
225 prediction.

226 **Case study demonstrations**

227 We apply this model to two case studies that are chosen to represent different geographic areas,
228 seasonal resolution, taxonomic focus, and inferential goals.

- 229 1. *Yellowtail flounder on Georges Bank*: The first case-study involves yellowtail flounder
230 (*Limanda ferruginea*) on Georges Bank, a shallow stretch of the continental shelf in the
231 Northwest Atlantic Ocean. This commercially important species is sampled by three bottom
232 trawl surveys that each provide a different snapshot of fish distribution and abundance. We
233 seek to answer: can we standardize data from multiple surveys to share information across
234 seasonal sampling programs and thereby predict density in unsampled times and areas?
- 235 2. *Copepods in the eastern Bering Sea*: The second case-study involves copepodite stage 3-6
236 abundance in oblique plankton tows from five meters above sea floor to water surface for
237 *Calanus marshallae/glacialis*. These copepods are a substantial component of diet for fish,
238 seabirds and marine mammals in the eastern Bering Sea (Livingston *et al.*, 2017). Copepods
239 undergo rapid population growth and decline during the annual sampling interval, and this
240 application is therefore useful to highlight the potential for a relatively fine resolution for

241 seasonal intervals. We seek to answer: can seasonally unbalanced sampling data be used to
242 identify changes in the seasonal timing of population densities; for example, to estimate the
243 seasonal match between larval fish and zooplankton prey?

244 We discuss each in more detail below (see Fig. 1 for seasonal and interannual variability in data
245 availability).

246 *Case study #1: Yellowtail flounder on Georges Bank*

247 Yellowtail flounder are a historically important component of the Georges Bank fishery and
248 ecosystem (Stone *et al.*, 2004), but are currently at low biomass due to low recruitment and
249 unexplained mortality of adults (Legault and McCurdy, 2018). Despite a large amount of age-
250 based data available for this stock, standard stock assessment models have performed poorly
251 with large retrospective patterns and were replaced with an index-based approach in 2014
252 (Legault *et al.*, 2014).

253 We compile sampling data for three bottom trawl surveys 1985-2017 (see Fig. S1): Spring
254 (March 24 – April 25) and Fall (Sept. 30 – Nov. 6) bottom trawl surveys conducted by the
255 Northeast Fisheries Science Center (NEFSC), and a bottom trawl survey by Department of
256 Fisheries and Oceans (DFO) Canada (Feb. 11 – March 29) (O’Boyle *et al.*, 1995; Politis *et al.*,
257 2014). The NEFSC Spring and Fall surveys switched vessels in 2009, and we use data converted
258 to units of the earlier survey based on paired intercalibration sampling (Miller *et al.*, 2010). By
259 contrast, the DFO survey gear has been consistent over time, and uses different protocols than
260 the earlier US survey, hence likely catching a different proportion of local abundance (termed
261 “catchability”) than the US surveys. Surveys also differ in their spatial footprint of sampling: the
262 US surveys follow a stratified random design that covers the entire stock boundary, while the

263 DFO survey uses a different stratified random design and samples only a subset of this spatial
264 area, avoiding the southwestern corner as well as moraine habitat in the western portion (Stone
265 and Gross, 2012).

266 Design-based indices of abundance are available for all three surveys, although we note that
267 the DFO design-based index is calculated only for the portion of the stock sampled by that
268 survey. We also fit an alternative multivariate spatio-temporal model, which treats each season
269 as a separate category and estimates independent spatial and spatio-temporal variation for each
270 season. This “default” specification is widely used in fisheries index-standardization (Thorson,
271 2019b), and therefore provides a reference-value for abundance indices calculated in a more
272 conventional manner.

273 The Georges Bank yellowtail flounder stock is defined for an area that straddles the Hague
274 Line separating the US and Canadian exclusive economic zones (EEZ), requiring a method to
275 allocate the total quota between the two countries. Swept area estimates from the three surveys
276 (DFO, NEFSC spring and NEFSC fall) are averaged, proportions on either side of the Hague
277 Line are calculated, and then a loess smooth is fit to the respective time series east/west. The
278 total annual quota is allocated between countries based on the terminal year smoothed proportion
279 of total stock biomass in US and Canadian waters (Murawski and Gavaris, 2004). Given the
280 importance of comparing estimates of abundance between DFO and US surveys, we seek to
281 develop an alternative model that can predict density using data from all surveys over the spatial
282 footprint of the stock assessment.

283 We use a model with annual and seasonal main effects for both intercepts and spatial
284 variation, using 250 knots to approximate spatial variables, and an autoregressive process for the
285 interaction of year and season. Initial runs of the full model showed that several variance

286 components were estimated to be zero, and we changed the model to avoid numerical problems
287 associated with a parameter estimated at a bound (i.e., an estimated variance of zero); see Table
288 S3 for details. The seasonal main effect for intercepts includes the effect of both seasonal
289 differences in density as well as differences in catchability among gears, and resulting density
290 estimates are not directly comparable among surveys due to this missing information regarding
291 catchability differences. We therefore display resulting abundance indices after scaling each
292 series to have a mean of 1.0 across years. We focus interpretation by displaying the
293 autocorrelated spatial variation in the season-year interaction, to demonstrate how this model
294 component allows information to be shared between seasons.

295 *Case study #2: Copepods in the eastern Bering Sea*

296 Copepods are an important component of secondary production in the Bering Sea, and occur in
297 stomach samples for a wide range of commercially important fishes (Livingston *et al.*, 2017).
298 Two species of copepod (*Calanus glacialis* and *C. marshallae*) co-occur in the eastern Bering
299 Sea and are difficult to identify to species, and we refer to them collectively as *C.*
300 *glacialis/marshallae* in the following (Campbell *et al.*, 2016). *C. glacialis/marshallae* has one
301 cohort per year in the eastern Bering Sea and is a key prey for multiple fish species in their first
302 year of life (Strasburger *et al.*, 2014). Productivity and spatial dynamics in this ecosystem are
303 strongly associated with wintertime sea-ice extent (Hunt *et al.*, 2011) and the resulting extent of
304 cold near-bottom waters (termed the ‘cold pool;’ Sigler *et al.*, 2011) during the summer growing
305 season for copepods (Eisner *et al.*, 2014, 2018; Kimmel *et al.*, 2018). Historically, zooplankton
306 sampling in the EBS occurred on process-oriented surveys, which varied year to year in their
307 spatial and temporal coverage. Recently, sampling has occurred more regularly in spring (late
308 April) and fall (late September) along the 70 m isobath from the southeastern Bering Sea M2

309 mooring location (56.87N, 164.05W) to the M8 mooring location (62.19N, 174.69W).
310 Additionally, zooplankton sampling has occurred in recent years along a grid in the southeastern
311 Bering Sea from the inner to outer shelf (~ 30-180 m) from 54.5 to 60 N in May and again in
312 August/September. We here restrict samples to oblique tows of a bongo net, starting near bottom
313 and ending near surface (see Fig. S2), and approximate spatial variation using 100 knots. These
314 oblique tows include a measure of total volume swept, and we divide the total number of
315 copepodite stage 3+ copepod (*Calanus glacialis/marshallae*) by volume swept, and then
316 multiply by the seafloor depth at the beginning of the tow to obtain vertically integrated
317 numbers-density. Using vertically integrated numbers-density as response-variable then allows
318 us to predict vertically integrated densities across a standard survey area, where the sum across
319 this survey area represents a prediction of vertical and spatially integrated abundance in numbers.
320 Future studies could instead include water-column height as an offset, and expand densities
321 while defining area, $a(s)$ in Eq. 10, as the product of surface-area and water-column height; we
322 leave this comparison as a topic of future research. *C. glacialis/marshallae* occur in 97% (3691
323 of 3802) of all available samples, and there is little information available to identify spatial,
324 temporal, or seasonal patterns in encounter probability. We therefore use a reduced model
325 wherein we remove all spatial and temporal variation in the first linear predictor (i.e., $n_i = n$ for
326 all locations s , seasons u , and years y), such that the model estimates a single encounter
327 probability for all samples, and focuses inference on the expected number of *Calanus*
328 encountered in each sample. The model again estimated several variance terms near zero, and
329 we eliminated terms with zero variance to avoid numerical difficulties (see Table S3 for details).

330 We specifically seek to measure interannual changes in *C. glacialis/marshallae* phenology.
331 To do so, we calculate the weighted average of seasonal intervals, where each season is weighted

332 by the total abundance in that season. This “abundance-weighted average season” statistic is
333 analogous to “center of gravity” (COG), which is calculated as the abundance-weighted spatial
334 location for a population; COG is widely used as a measure of spatial distribution shifts (Pinsky
335 and Palumbi, 2013; Thorson *et al.*, 2016a). We specifically calculate abundance-weighted
336 average season $\bar{u}(t)$ as:

$$\bar{u}(y) = \sum_{t \in \mathbf{t}_y} \left(\frac{D(t)}{D_y} \times u_t \right) \quad (11)$$

337 where \mathbf{t}_y is the vector of season-year indices t in year y , u_t is the season corresponding to
338 season-year t , D_y is the area-weighted sum of densities across locations and seasons in year y ,
339 $D_y = \sum_{t \in \mathbf{t}_y} D(t)$, and $D(t)$ is defined in Eq. 10. Standard errors for $\bar{u}(t)$ are again calculated
340 using the generalized delta-method. This index does not measure “peak abundance” *per se*, but
341 instead measures years when *C. glacialis/marshallae* abundance is high in early or later portions
342 of the summer growing season. Given the known climate-sensitivity of copepod production in
343 the Bering Sea, we compare our phenology estimate with the summertime areal extent of the
344 cold pool (waters < 2 °C) on the EBS shelf (Robert Lauth, personal communication) as measured
345 using temperature sensors deployed on bottom trawl gear in the eastern Bering Sea (Lauth and
346 Conner, 2016).

347 Finally, we explore the sensitivity of the abundance-weighted average season $\bar{u}(t)$ to the *a*
348 *priori* specification of the number of seasonal intervals that are modeled in each year. To do so,
349 we contrast results from our model using month-long intervals (nine seasonal-intervals per year
350 after excluding months with no sampling) with either aggregating all samples into Spring (Feb.-
351 May) and Summer/Fall (June-Oct.) seasons (two seasons per year), or aggregating samples into

352 two-week intervals (18 seasonal intervals per year with data). For each of these seasonal
353 specifications, we fit the same seasonal spatio-temporal model and compare resulting estimates
354 of $\bar{u}(t)$; we hypothesize that either month-long or biweekly intervals will be sufficiently fine-
355 grained to yield similar results, while the two-season model will have such coarse seasonal
356 resolution that it will likely result in different estimates than the other two models.

357 **Results**

358 We use the same seasonal spatio-temporal model for both case studies (see Fig. S3 for
359 triangulated meshes in each example). However, we use this model for very different inference
360 in each case study, and therefore address them separately below.

361 **Georges Bank yellowtail flounder: Inferring seasonal variation in unsampled habitat**

362 We first compare total abundance of yellowtail flounder on Georges Bank in each of three
363 seasons, estimated using the seasonal spatio-temporal model with either a design-based index or
364 a simpler spatio-temporal model that is run independently for each season (Fig. 2). This
365 comparison shows that the two model-based indices have similar estimates of total abundance,
366 and differ more from the design-based index for DFO. We note that the design-based index for
367 DFO has a large spike in 2008/2009, and this spike is not represented in either model-based
368 index. Model exploration shows that this spike arose from one sample in each of those years
369 wherein the DFO survey caught an anomalously large quantity of yellowtail flounder. The
370 model-based indices both treat these observations as “outliers” relative to the weighting used by
371 the design-based estimator, and hence these samples have less statistical leverage in the model-
372 based than the design-based index.

373 We next explore the ways in which the seasonal spatio-temporal model shares information
374 among seasons. The largest consequence is that it extrapolates the DFO index back to
375 1985/1986, when there was no DFO sampling (see Fig. 2 top panel and Fig. S1). This
376 extrapolation is based on the main effects of season and year for both intercepts and spatial
377 variation, such that the index in those years is “shrunk” towards the approximately stable trend in
378 abundance seen in the other seasons in that year; the extrapolation also results in an increase in
379 standard errors (width of blue shaded area) in those years relative to others. We also highlight
380 the consequence of autocorrelation ($\rho_{n\epsilon} = 0.85$ and $\rho_{w\epsilon} = -0.19$; see Table 1) on estimated
381 spatio-temporal variation arising across seasons and years (Fig. 3). In 1989-1992, for example,
382 the spring and fall surveys both encountered an increase in density relative to long-term averages
383 in the southwestern stock area, where DFO sampling does not occur. This hot spot is estimated
384 to occur starting in fall 1989, and persists consecutively through 1990 and into the DFO survey
385 in 1991, before largely reverting to long-term densities by the spring survey in 1991. These and
386 other examples of autocorrelated season-year variation cause the seasonal model to shrink
387 estimates in areas lacking samples towards their estimates in other seasons with more spatially
388 comprehensive sampling.

389 **Eastern Bering Sea copepods: Measuring interannual variation in phenology**

390 We next explore the behavior of the seasonal model when applied to a case study with more
391 seasons (nine intervals each lasting one month). This case-study exhibits an extremely
392 unbalanced sampling design across seasons (see bottom panel of Fig. 1), where the majority of
393 sampling is available in either April-May or Aug.-Sept. We start by illustrating *C.*
394 *glacialis/marshallae* density estimates in four selected years (Fig. 4, showing
395 1994/2002/2007/2012). Later years (2007/2012) are selected to show the impact of the spatially

396 distributed sampling design in May and Aug.-Oct. that is currently implemented in the eastern
397 Bering Sea, while earlier years (1994/2002) are selected to show the relatively opportunistic
398 sampling that occurred in these years (see Fig. S2 for spatial coverage of sampling across all
399 years). Density plots (Fig. 4) again show the role of autocorrelated season-year effects ($\rho_{wE} =$
400 0.72; see Table 1) on model performance where, for example, the spatial configuration of high-
401 density areas in 2012 is essentially interpolated between May and August, given that sampling
402 data are sparse between these two months. Alternatively, years with few sampling data in any
403 month (e.g., 1994) are shrunk towards the estimate of the season main-effect, where the model
404 typically estimates increased densities and a broader distribution of high-density habitats in June-
405 July relative to early (Feb.-April) or late (Sept.-Oct.) months.

406 We next illustrate abundance indices across seasons for each year (Fig. 5), which confirms
407 that the seasonal main-effects are estimated to follow a dome-shaped pattern in *C.*
408 *glacialis/marshallae* density with a peak in June-July (as shown in 1996/2001, when data are
409 particularly sparse). As noted in the Methods section, this dome-shaped pattern is not specified
410 within the estimation model, and instead arises purely from average patterns seen in the data.
411 Similarly, the action of the year main-effect is also apparent. For example, sampling in April
412 1994 yields elevated density relative to its spatial and seasonal expectation and the model
413 therefore predicts elevated density for all seasons in that year. By contrast, sampling in August
414 2002 yielded lower densities than the average for its season and location, resulting in an estimate
415 of low density for that entire year. In these years with seasonally restricted sampling (e.g.,
416 1993/2002), the confidence intervals are relatively wide compared with years with seasonally
417 distributed sampling (e.g., 2007-2012).

418 Finally, we compute the abundance-weighted average season for *C. glacialis/marshallae* in
419 the eastern Bering Sea (Fig. 6). Standard errors are sufficiently small to detect interannual
420 variation in phenology (e.g., where 2003 is earlier than 2007) during years with seasonally
421 distributed sampling (approximately 2003 onward), while intervals are much wider in earlier
422 years. The predicted index across all years ranges between mid-June to late July, and therefore
423 spans nearly 45 days. As expected, the index is positively correlated (Pearson correlation = 0.60)
424 with cold-pool extent, where “warm years” (those with a small cold pool) are estimated to have
425 earlier average copepod phenology and vice-versa for “cold years” with a large cold pool. The
426 index is similar when specifying 18 biweekly seasonal intervals (Fig. S4). Indices from these
427 two models are also correlated with the index estimated using two (Spring vs. Summer/Fall)
428 seasonal intervals, although the latter model does not yield an interpretable scale for variation
429 among years due to the coarse resolution of seasonal intervals.

430 **Discussion**

431 In this study, we have demonstrated how a seasonal spatio-temporal model can be constructed to
432 account for spatially and seasonally unbalanced sampling data. We used two contrasting case
433 studies to show that this seasonal spatio-temporal model can yield information that is useful for
434 both ecological insight as well as applied fisheries management. We first discuss each of these
435 case studies in detail, and then speculate about other potential applications.

436 Our first case study focused on inferring interannual changes in resource abundance for a
437 commercially important fish while accounting for spatial areas that are regularly sampled by
438 some but not all seasonal surveys. This situation is common in many transboundary
439 negotiations, for example, for fisheries in the North Sea (Pedersen and Berg, 2017), although the

440 yellowtail flounder case-study had a unique difficulty of involving different spatial coverage for
441 data in each season. While both the NEFSC surveys and the DFO survey have a stratified
442 random design, the DFO survey has a higher sampling rate in Canadian waters than US waters
443 (see Fig. S1). In particular, the portion of the DFO survey used in the Georges Bank yellowtail
444 flounder assessment does not cover the southwest portion of the bank, which is covered by the
445 two NEFSC surveys. There are DFO survey strata in this area, but this area often does not
446 contain sample locations due to the low sampling rate or is dropped entirely when the survey has
447 to end early due to weather or vessel troubles. These practical and logistical factors are common
448 in bottom trawl surveys and lead to imbalanced sampling and coverage among surveys. Applying
449 a seasonal spatio-temporal model provides a statistically sound approach to combining the
450 information from the multiple surveys; we showed that it is useful specifically to infer hot spots
451 in density in unsampled areas and times based on sampling occurring in other seasons. This may
452 be particularly important when the spatial distribution of biomass is estimated for areas that
453 differ from the survey stratification, as in the quota allocation sharing agreement for this stock.

454 By contrast, the second case study focused on inferring interannual variation in phenology
455 for two pelagic crustacean species using vertically integrated tows from many different sampling
456 programs, each with different seasonal timing and spatial distribution. Resulting estimates of
457 abundance-weighted average season showed a clear and statistically significant association
458 between phenology and oceanographic conditions, while allowing comparison of phenology
459 across years with greatly different seasonal data availability. Numerous studies have shown that
460 *C. glacialis/marshallae* populations have peak abundance in June and July (e.g., Eisner et al.
461 (2018) using data from 2008-2010), and also respond to interannual variability in temperature on
462 the southeastern Bering Sea shelf (Baier and Napp, 2003; Coyle *et al.*, 2008; Eisner *et al.*, 2014,

463 2018; Coyle and Gibson, 2017; Kimmel *et al.*, 2018). In years with early ice retreat, *C.*
464 *glacialis/marshallae* that emerge from diapause will experience a potential mismatch with the
465 spring phytoplankton bloom that occurs later during warm years (Brown and Arrigo, 2013;
466 Sigler *et al.*, 2014, 2016). This mismatch combined with warmer temperatures that accelerate
467 development, appears to reduce *C. marshallae/glacialis* abundances and they typically have low
468 abundance by mid-August to late September in warm years, perhaps due to entry into diapause
469 (Kimmel *et al.*, 2018). During years of late ice retreat, by contrast, *C. glacialis/marshallae*
470 benefits from the presence of ice-associated algae that are grazed heavily to fuel egg production
471 (Campbell *et al.*, 2016). Cooler temperatures slow development rates and allow accumulation of
472 individuals that persist on the shelf due to a delay of entry into diapause (Coyle and Gibson,
473 2017; Kimmel *et al.*, 2018). Continued warming of ocean waters is expected to impact
474 phenology of *Calanus* by shifting the timing of emergence and exit into diapause (Wilson *et al.*,
475 2016). Long-term warming has already caused earlier appearance of *C. glacialis* in the White
476 Sea (Persson *et al.*, 2012; Usov *et al.*, 2013) and *C. finmarchicus* in Svalbard and northern
477 Iceland (Espinasse *et al.*, 2018).

478 Improved information regarding seasonal timing derived from seasonal spatio-temporal
479 models could be useful for a wide variety of ecosystem studies and management questions. In
480 the eastern Bering Sea, for example, the abundance of *C. marshallae/glacialis* during the fall is
481 associated with walleye pollock (*Gadus chalcogrammus*) condition and early-life survival
482 (Heintz *et al.*, 2013; Siddon *et al.*, 2013; Eisner and Yasumiishi, 2018). Notably, positive
483 significant linear relationships have been found between late summer abundances of large
484 copepods, and abundances of age-3 pollock three years later when they enter the fishery (Eisner
485 and Yasumiishi, 2018). By estimating how phenology of *C. glacialis/marshallae* varies from

486 year to year, this study shows that changes in phenology likely contribute to interannual variation
487 in late summer abundance. Detecting changes in phenology can affect the seasonal timing of
488 spawning migrations and therefore the interpretation of pre-season test fisheries (Flynn and
489 Hilborn, 2004).

490 In addition to being useful for detecting changes in phenology, the approach described here
491 could be useful for standardizing survey indices that are potentially biased by seasonal changes
492 in abundance or distribution. For instance, for taxa, stages, or processes that develop rapidly in
493 time and vary over space (e.g., zooplankton, larval fish, and squid abundance) small changes in
494 survey timing can result in biased estimates of abundance. Seasonal spatial-temporal models
495 could be used to control for survey timing and extent. In a similar vein, fisheries scientists
496 continue to use catch-per-unit-effort from fishery data to index changes in fish abundance.
497 Previous research has shown how spatio-temporal models can be used to control for interannual
498 variation in the spatial distribution of fishing (Thorson *et al.*, 2017; Grüss *et al.*, 2019), but there
499 has been less focus on controlling for differences in spatial distribution occurring at finer
500 seasonal scales than quarterly (i.e., >4 seasons per year). Seasonal fishery data could be
501 particularly useful in conjunction with resource surveys, for example, where a seasonal spatio-
502 temporal model could be fitted to both data sources to index changes in phenology that affect the
503 proportion of fish that are available to a given survey (Nichol *et al.*, 2019). In addition, such an
504 approach could be used to study how seasonal shifts in distribution are changing in response to
505 climate, which may in turn affect availability to resource users or be useful as an environmental
506 index within a stock-assessment model.

507 Results are complementary to the growing worldwide effort to document changes in the
508 spatial distribution of fishes and many other taxa (Anderson *et al.*, 2009). In fishes, the rate of

509 climate-driven shift in distribution is often measured using “center of gravity,” ; that is, the
510 centroid of the distribution measured as latitude, longitude, depth, or other location measures
511 (Pinsky *et al.*, 2013; Thorson *et al.*, 2016a; Currie *et al.*, 2019). Center of gravity is a useful
512 measure for comparing rates of climate-driven distribution shifts across regions but does not
513 capture specifics about the density available to individual fishing ports or other partitions of
514 available habitat (Rogers *et al.*, 2019; Selden *et al.*, 2020). Similarly, we use abundance-
515 weighted average season as a measure of seasonal timing for available copepod prey; this
516 follows similar practice measuring changes in phenology using a population average (Rogers and
517 Dougherty, 2019). While this aggregate measure of timing does not indicate total abundance or
518 availability in specific seasons, we believe that this metric will provide a useful basis for
519 comparisons of climate-driven shifts in phenology among regions, and hope that having a
520 standardized measure facilitates future comparative research.

521 We note that seasonal spatio-temporal models also generate a new set of interesting questions
522 to resolve when using results. For example:

- 523 1. Is the spring, fall, or DFO index of yellowtail flounder abundance most appropriate to
524 include when fitting a stock assessment model, or perhaps some average of these different
525 surveys?
- 526 2. Is late summer/fall abundance of *C. glacialis/marshallae* the best predictor of pollock
527 recruitment, or instead the abundance of *C. glacialis/marshallae* across all seasons within a
528 given year (the area under the curve in each panel of Fig. 5)?
- 529 3. Is abundance-weighted average season the best metric for measuring changes in phenology,
530 or is it better to measure changes in the seasonal timing of emergence/disappearance of

531 copepods, analogous to measuring leading/trailing edges in spatial measures of distribution
532 (Anderson *et al.*, 2009)?

533 These and other questions become apparent when explicitly accounting for seasonal variation
534 within spatio-temporal models, and the solution will obviously depend upon how results are
535 being used. Thus, these models open up new opportunities for study, as well as challenges for
536 interpretation. We therefore argue that analysts should communicate clearly about how they
537 interpret seasonal variation in any future applications of the seasonal spatio-temporal model. We
538 also note that developing sensitive diagnostics for model mis-specification, and simulation-
539 testing the likely performance of spatio-temporal models is an ongoing endeavor. The package
540 VAST used here has been simulation-tested elsewhere (Grüss *et al.*, 2019; Johnson *et al.*, 2019;
541 Thorson *et al.*, 2019; Brodie *et al.*, 2020), but we recommend ongoing, independent testing to
542 understand the potential impacts of model mis-specification. Importantly, new forms of mis-
543 specification are plausible in seasonal models, e.g., varying rates of temporal change and/or
544 spatial clustering in different seasons.

545 Given rapid changes in climate and its effects on the timing of seasonal processes of growth,
546 migration, mortality, and reproduction, approaches for modeling processes that can handle
547 seasonal and spatial processes are increasingly needed. We foresee a wide range of future
548 applications for spatial models that include both seasonal and interannual variation. The model
549 is implemented generically within publicly available software that also includes capacity for
550 multivariate analysis, climate-linkages, and skillful near-term forecasting (Thorson, 2019b). We
551 hope that future users will contribute to documenting the benefits and drawbacks of this
552 promising class of models for ecosystem science and management.

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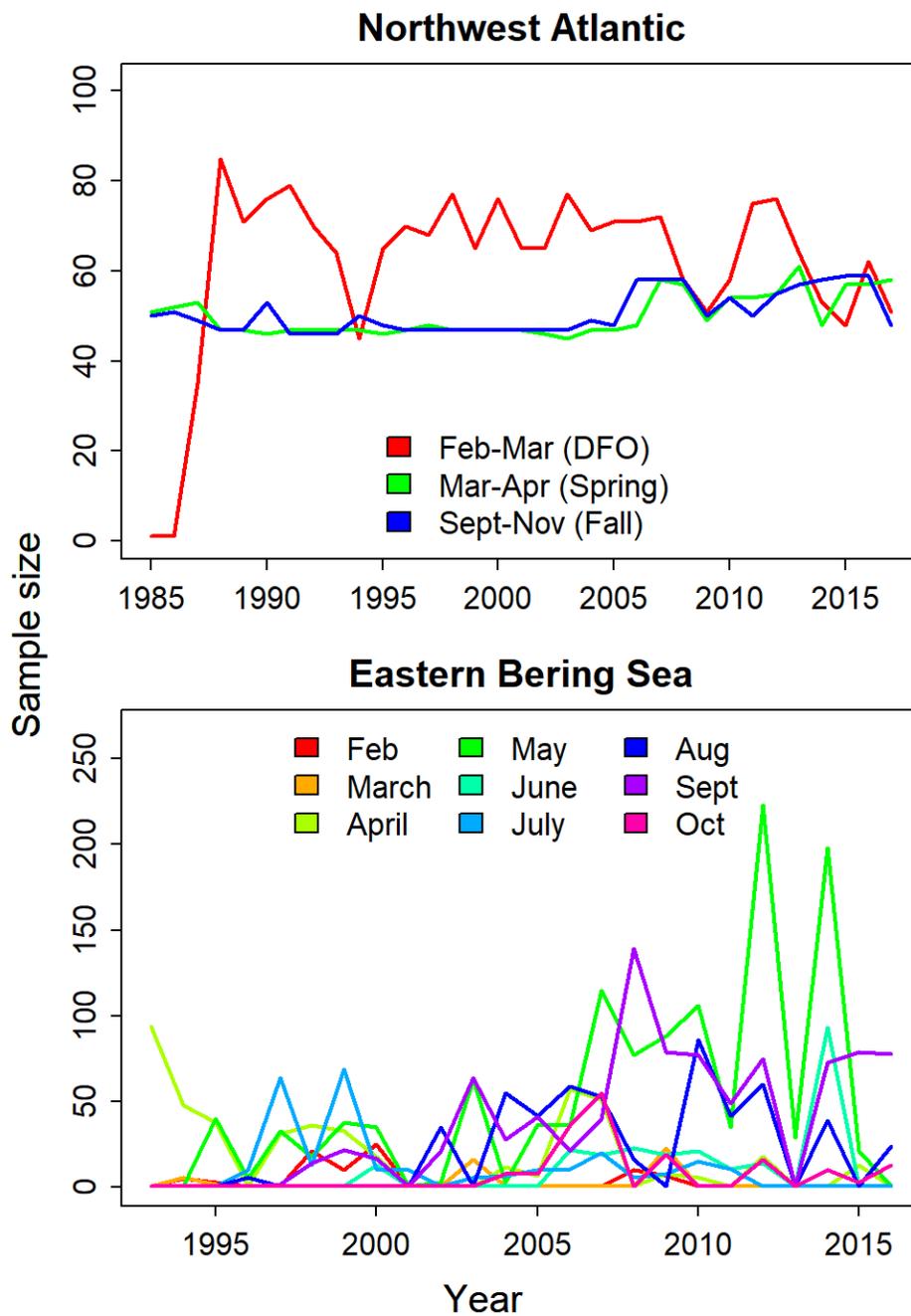
779 Table 1 – List of estimated parameters (and associated symbols) governing spatial and temporal
780 variance (listing estimate “Est.” and standard error “SE”) for each case-study application; this
781 corresponds to all estimated fixed effects except intercepts μ_β , $\beta_{nu}(u)$, and $\beta_{ny}(y)$. Parameters
782 listed as “-“ correspond to terms that are dropped due to the corresponding variance approaching
783 zero (see Table S3 for details). Note that the eastern Bering Sea application does not include
784 spatial or temporal variation in the first linear predictor, due to a near 100% encounter
785 probability; linear transformation **H** governing geometric anisotropy involves estimating two
786 parameters which are listed first for each case-study.

Parameter	Symbol	Northwest Atlantic		Eastern Bering Sea	
		Est.	SE	Est	SE
Parameter #1 in H	-	0.264	0.083	0.421	0.082
Parameter #2 in H	-	0.571	0.097	-0.221	0.088
SD for spatial variation in n	$\sigma_{n\omega}$	1.76	0.182	-	-
SD for spatial season-year interaction in n	$\sigma_{n\varepsilon}$	0.47	0.05	-	-
Natural log. for decorrelation rate in n	$\ln(\kappa_n)$	-3.296	0.096	-	-
SD for intercept season-year interaction in n	$\sigma_{n\beta}$	-	-	-	-
Autocorrelation for intercepts in n	$\rho_{n\beta}$	-	-	-	-
Autocorrelation for spatial season-year interaction in n	$\rho_{n\varepsilon}$	0.874	0.031	-	-
Natural log. for SD in spatial season and year effects in n	$\ln(\sigma_{n\xi})$	-0.638	0.135	-	-
SD for spatial variation in w	$\sigma_{w\omega}$	0.479	0.069	1.481	0.170
SD for spatial season-year interaction in w	$\sigma_{w\varepsilon}$	0.89	0.063	1.039	0.055
Natural log. for decorrelation rate in w	$\ln(\kappa_w)$	-2.567	0.116	-4.488	0.063
SD for intercept season-year interaction in w	$\sigma_{w\beta}$	-	-	-	-
Autocorrelation for intercepts in w	$\rho_{w\beta}$	-	-	-	-
Autocorrelation for spatial season-year interaction in w	$\rho_{w\varepsilon}$	-0.149	0.085	0.721	0.034
Natural log. for SD in spatial season and year effects in w	$\ln(\sigma_{w\xi})$	-	-	-0.644	0.163
Natural log. for SD of measurement error	$\ln(\sigma_m)$	-0.133	0.04	-0.103	0.017

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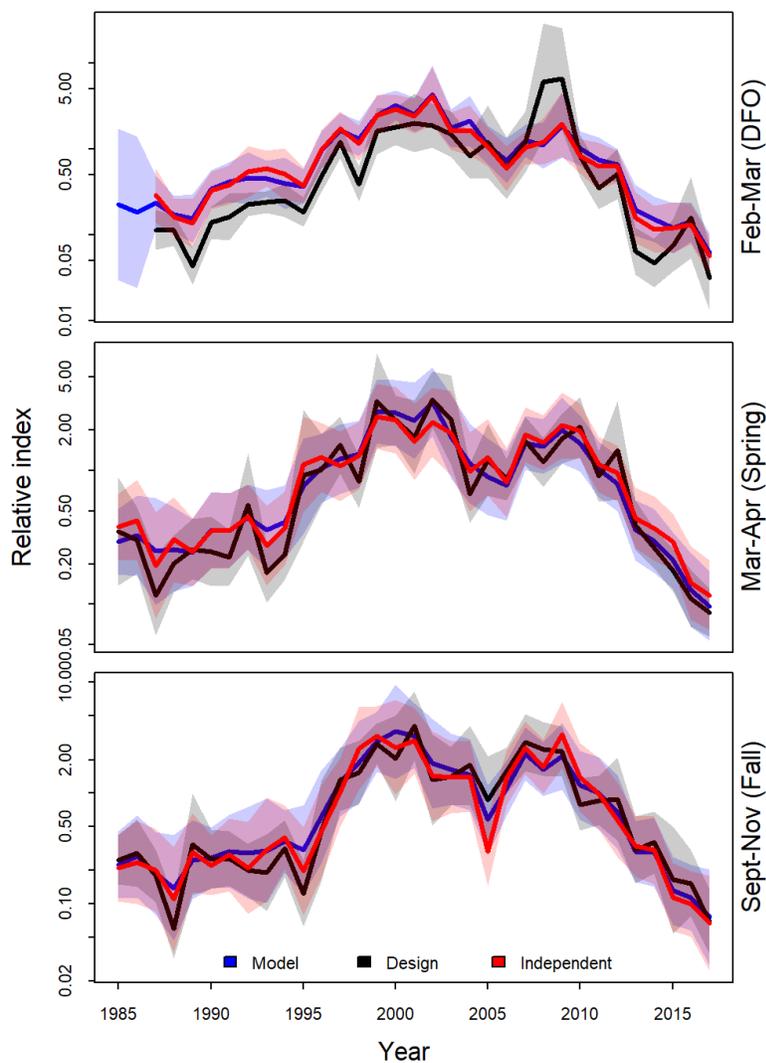
789 Fig. 1 – Data availability (y-axis) for season (colored line) and each year (x-axis) for case-studies
 790 in the Northwest Atlantic Ocean (top panel) and eastern Bering Sea (bottom panel), where the
 791 colorbar for each season is indicated in each legend.



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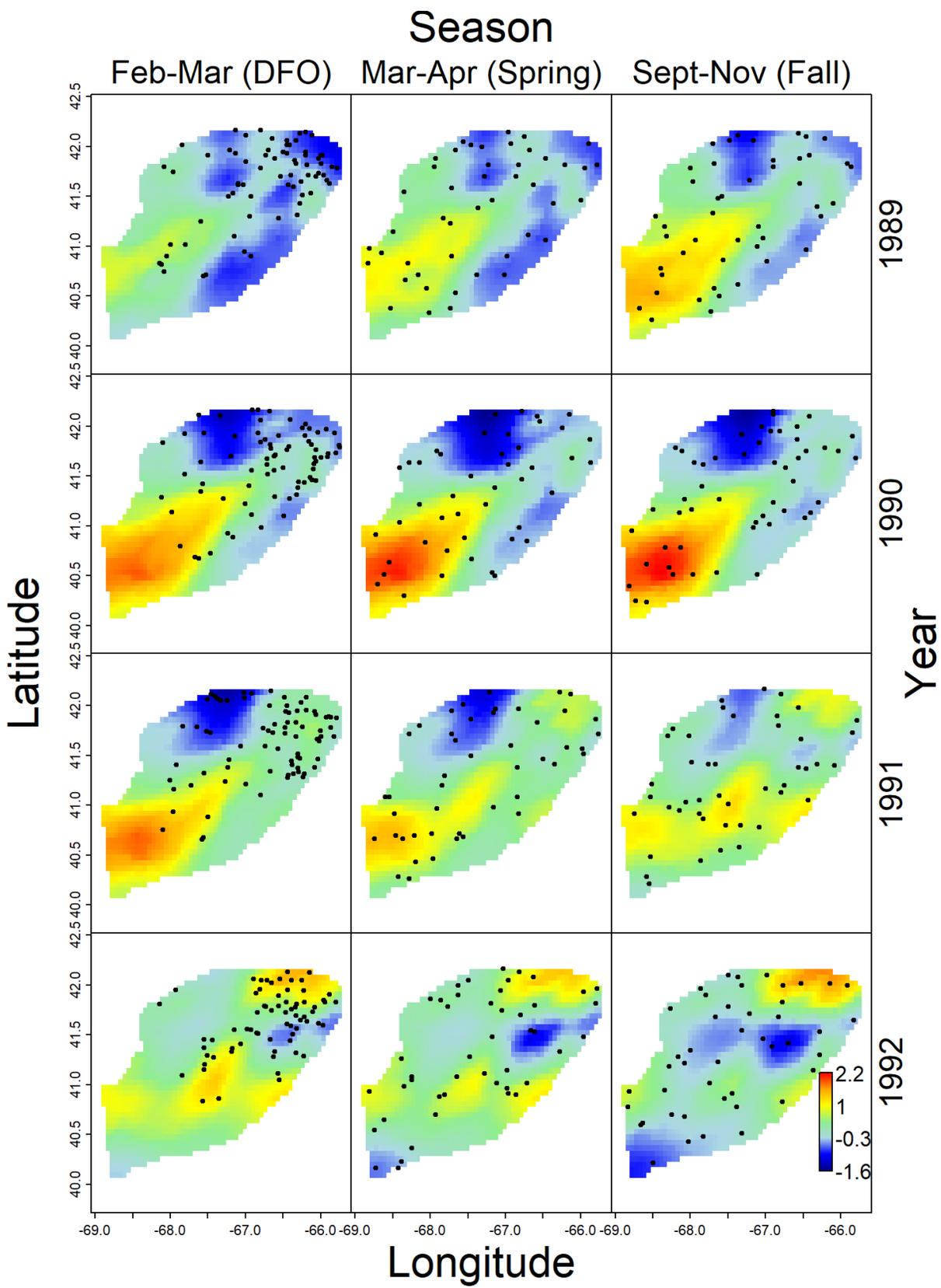
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794 Fig. 2 – Index of relative abundance (y-axis using log-scale; scaled to have mean of 1 across
 795 years) for a design-based index (black line), seasonal spatio-temporal model (blue line), or
 796 independent spatio-temporal model (red line) including +/- 1 standard error (shaded interval) of
 797 yellowtail flounder for 1985-2017 (x-axis) for each of three seasons (DFO, as well as spring and
 798 fall NEFSC bottom trawl surveys). Note that the design-based and independent spatio-temporal
 799 models cannot estimate abundance for the DFO survey in 1985/1986, and therefore have no
 800 estimates for those years (top panel)

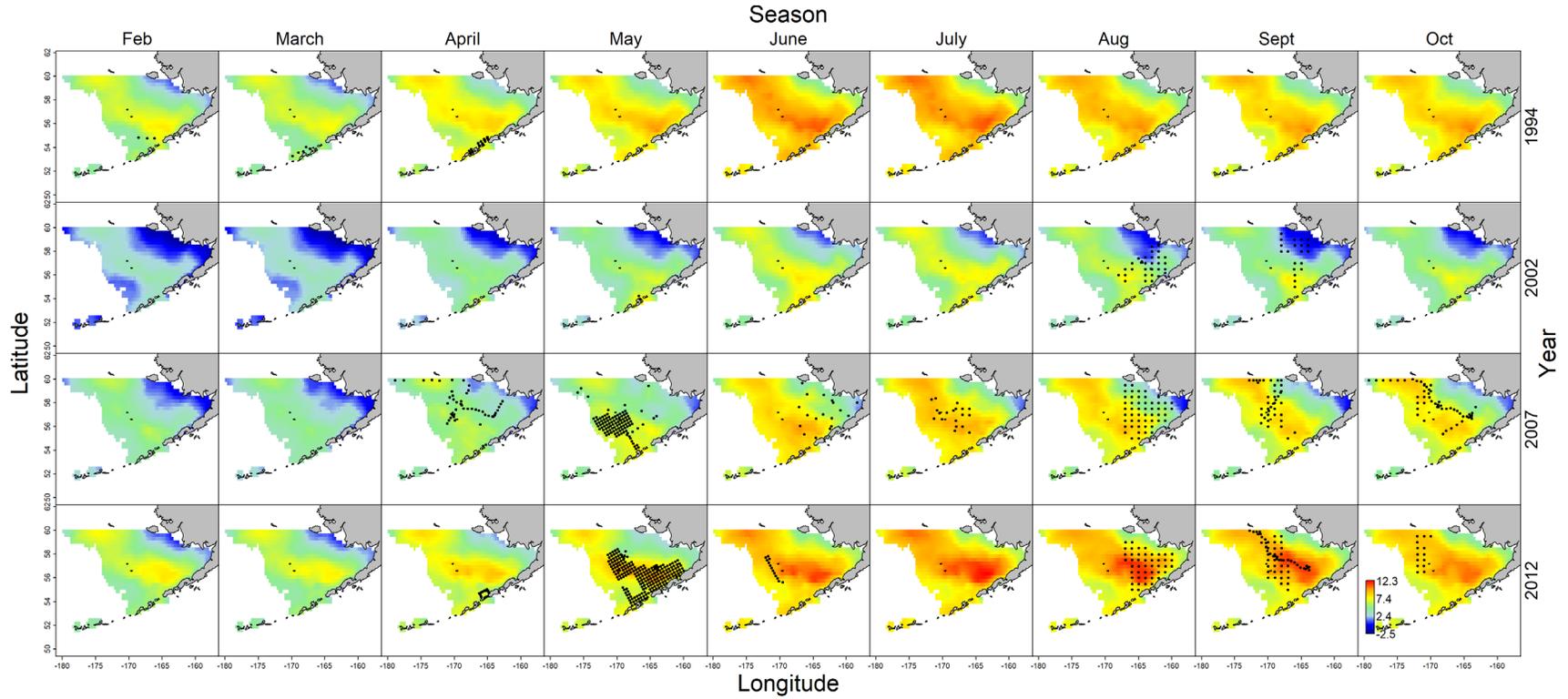


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802 Fig. 3 – Spatio-temporal variation in the log-linked linear predictor for numbers-density $\varepsilon_n^*(s, t)$
803 for each location s and year-season interval t for yellowtail flounder on Georges Bank in the
804 Northwest Atlantic Ocean for 1989-1992 (rows) of the 24 modeled years (1985-2017) and three
805 seasonal surveys (columns) in each year (DFO Feb.-March, NEFSC Spring March-April, and
806 NEFSC Fall Sept.-Nov. surveys). Each panel also shows the location of available data in that
807 season and year (black dots), which highlights the absence of data from DFO in the southwestern
808 portion of the stock area. Years are selected to highlight the estimates of increased density in the
809 DFO survey in the southwestern portion 1990-1991 which is not sampled by that survey; this
810 estimated hotspot is informed by sharing information among surveys. The use of a log-linked
811 linear predictor means, for example, that a location s and year-season t with a value of
812 $\varepsilon_n^*(s, t) = 0.1$ has an approximately $\exp(0.1) = 10.5\%$ higher prediction of numbers-density
813 $n^*(s, t)$, while a location and time where $\varepsilon_n^*(s, t) = 1.0$ has an approximately $\exp(1.0) = 172\%$
814 higher prediction of numbers-density $n^*(s, t)$ than the value otherwise expected for that location
815 and time.



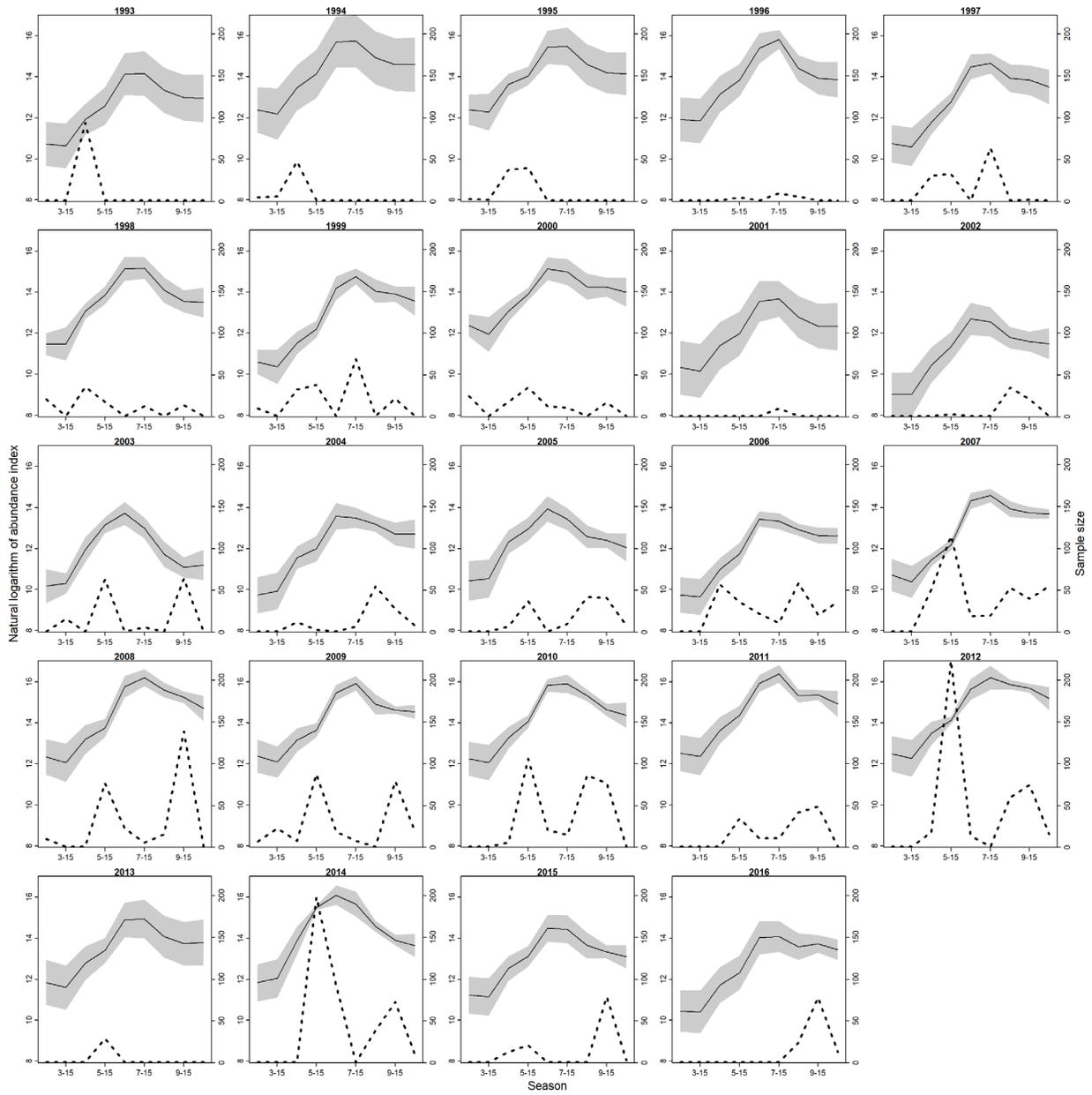
819 Fig. 4 – Natural logarithm of estimated density (vertically-integrated from 5 meters above seafloor to surface), $\ln(\text{number} \cdot \text{km}^{-2})$,
820 for copepodite stages 3+ *Calanus marshallae/glacialis* for four selected years (rows) from 24 analyzed years (1993-2016) and nine
821 month-long intervals in each year (columns). Each panel also shows the location of available data in that season and year (black dots).



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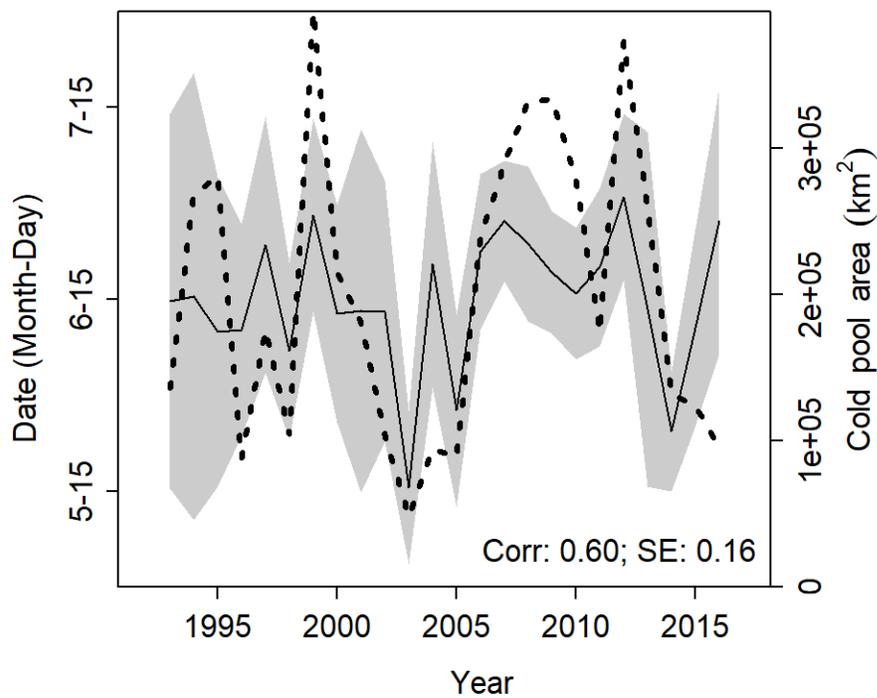
824 Fig. 5 – Natural logarithm of estimated total abundance (left-hand y-axis) for copepodite stage
825 3+ *Calanus marshallae/glacialis* in Feb.-Oct. (x-axis) for each year (panels) from 1993-2016,
826 estimated using a seasonal spatio-temporal model. Each panel shows an estimate (black line) +/-
827 one standard error (grey shaded interval), and also shows the sample size for each season (dashed
828 line; using right-hand y-axis). Note that the left and right-hand y-axes have identical range for
829 all panels, but abundance (left-hand y-axis) is in log-space while sample size (right-hand y-axis)
830 is in natural space.



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832

833 Fig. 6 – Estimate of abundance-weighted average season (calculated using Eq. 11; black line
834 with +/- one standard error as grey shaded area; scale on left-hand y-axis) in every year 1993-
835 2016 based on density estimates in every month Feb.-Oct. (x-axis) from a seasonal spatio-
836 temporal model compared with the summertime spatial extent of cold ($\leq 2^{\circ} C$) near-bottom
837 waters in the eastern Bering Sea (dashed line, “cold pool extent”; scale on right-hand y-axis).
838 We also show the Pearson correlation between cold-pool extent and the abundance-weighted
839 average season, as well as the standard error for this correlation based on 100 correlation values
840 calculated when simulating densities from the joint precision of fixed and random effects
841 (bottom right).



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